

# Exposing the P value fallacy to young residents

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# The $P$ value fallacy

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  - Goodman S. A dirty dozen: twelve  $p$ -value misconceptions. *Semin Hematol.* 2008;45:135-40
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- We devised a simple intervention to improve understanding of the  $p$  value and to promote the use of the Bayes Factor
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# Does the P value matters to you?

Do you know enough about the P value?	93%
Average patients per day	8 ± 1
Average articles read per week	4 ± 1
Do you see the P as the main parameter of a result?	75%
Average drug reps contacts per week	3.2 ± .3
Do the drug reps present sponsored research?	100%
Do the reps present the P value as the main result?	93%



# What does a p value of 0.05 mean?

## Multiple answers accepted

- 1 If there is no difference, the probability of getting this or a more extreme result is 5%
- 2 The probability that there is no difference is 5%
- 3 The probability that the groups are different is 95%
- 4 The minimum difference between the groups is 5%
- 5 If repeating the experiment, the probability of obtaining again the same result is 5%
- 6 I have no idea



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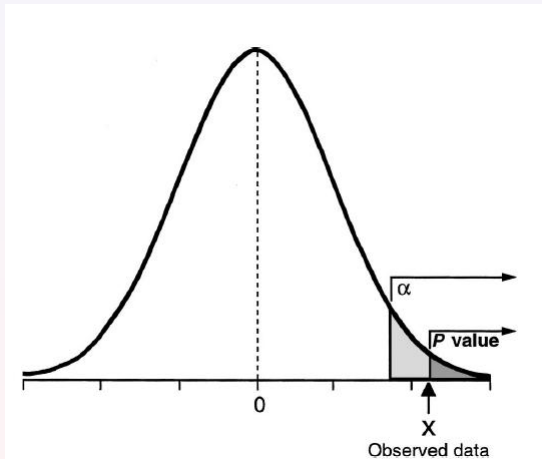
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# Definition of the P value



The probability of obtaining a test statistic at least as extreme as the one that was actually observed, assuming that the null hypothesis is true.



# What does a p value of 0.05 mean?

## Possible answers

The probability if there is no difference is 5%	2
The probability that there is no difference is 5%	7
The probability that there is a difference is 95%	11
The minimum difference is 5%	1
The probability of obtaining again this result is 5%	2
I have no idea	2



## What a P of 0.05 means...

- Imagine that you came home, and the light is on.
- You want to guess whether someone is in when the light is on
- A P of 0.05 is like knowing that when nobody is in (the null hypothesis), the light is on only 5% of the times
- Does this mean that there is a 95% probability that somebody is in?



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Is somebody in?

	No	Yes	
Off	95	?	
On	5	?	$?(5+?)$
$P \rightarrow$	5%		<b>but you want this<math>\uparrow</math></b>

- The P is the probability of finding the light on when nobody's in ( $L|P$ )
- But you want the probability that nobody is in when the light is on ( $P|L$ )



Is somebody in?

	No	Yes	
Off	95	?	
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# Bayes Factor (Likelihood ratio)

$$\text{Minimum BF} = \%TP/\%FP = e^{Z^2/2} = e^{1.96^2/2} = 6.8$$

Is somebody in?

	No	Yes	
Off	95	$100 - 32 = 68$	
On	5	$5 * 6.8 = 32$	$32/37 = 86\%$
	100	100	
P →	5%	32%	



Is somebody in?

	No	Yes	
Off	95	20	
On	5	80	$80/85 = 94\%$
	100	100	
P ->	5%	80%	

- In many experiments, the statistical power is selected to have a false negative rate ( $\beta$ ) of 20% and a false positive rate ( $\alpha$ ) of 5% (under certain assumptions *a priori*)



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## Post-intervention

- Many got confused by the abstraction
- In retrospect, a diagnostic example could have been better (e.g. nausea and pregnancy)
- After the course all except two identified the meaning of the P value
- All except one declared that in the future they would use the Bayes Factor instead.
- After 3 months, no one has ever done it



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- The P value is frequently used by drug reps to promote the results of drug trials and by young residents for interpreting them.
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